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## On an Additive Problem with Squarefree Numbers

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An asymptotic formula for the number of representations of a positive integer  $N$  in the form  $q_1 + q_2 + [\alpha q_3]$  is obtained, where  $q_1, q_2, q_3$  are squarefree numbers and  $\alpha > 1$  is a fixed irrational algebraic number.

*Key words:* ternary problem, squarefree numbers, asymptotic formula.

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