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## On Poisson Customary Polynomial Identities

S. M. Ratseev

Ulyanovsk State University, 42, Leo Tolstoy str., 432017, Ulyanovsk, Russia, RatseevSM@mail.ru

We study Poisson customary and Poisson extended customary polynomials. We show that the sequence of codimensions  $\{r_n(V)\}_{n \geq 1}$  of every extended customary space of variety  $V$  of Poisson algebras over an arbitrary field is either bounded by a polynomial or at least exponential. Furthermore, if this sequence is bounded by polynomial then there is a polynomial  $R(x)$  with rational coefficients such that  $r_n(V) = R(n)$  for all sufficiently large  $n$ . We present lower and upper bounds for the polynomials  $R(x)$  of an arbitrary fixed degree.

*Key words:* Poisson algebra, variety of algebras, growth of a variety.

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