# On a Particular Equivalent of Extended Riemann Hypothesis for Dirichlet $L$-functions on Numerical Fields

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A condition on summatory function over a set of prime ideals for Dirichlet $L$-functions on numerical fields is obtained. This condition is equivalent to extended Riemann hypothesis. Analytical properties of Euler products associated with this equivalent are studied.

*Key words:* extended Riemann hypothesis, Dirichlet $L$-functions, numerical fields.

## References

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